

# Intro to Physical Side Channel Attacks

Thomas Eisenbarth

15.06.2018

Summer School on Real-World Crypto & Privacy  
Šibenik, Croatia



UNIVERSITÄT ZU LÜBECK  
STIFTUNGSUNIVERSITÄT  
SEIT 2015



WPI

# Outline

- **Why physical attacks matter**
- Implementation attacks and power analysis
- Leakage Detection
- Side Channel Countermeasures

# Train Theft of MoD Laptop

**Train theft of MoD laptop with fighter secrets alarmed Pentagon:**

[...] a laptop was stolen containing secrets of the biggest military procurement project ever launched [...]. It held details of progress on the development of the United States' supersonic joint strike fighter. [...]

A petty thief stole the laptop from a British military officer at Paddington station in London last May.

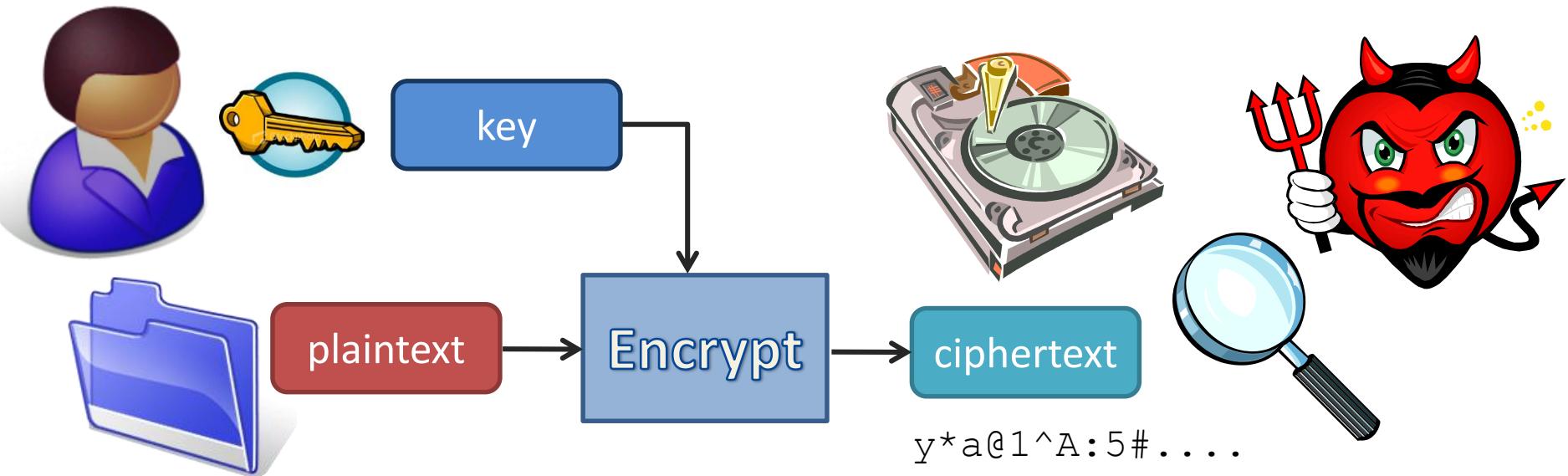
**It had been left on the luggage rack on a train.** [...]

**The computer is believed to have passed through several hands before it was returned to the Ministry of Defence.** The thief was caught and later convicted. [...]

**The Guardian, Tuesday 6 February 2001:**



# Solution: Hard Disk Encryption

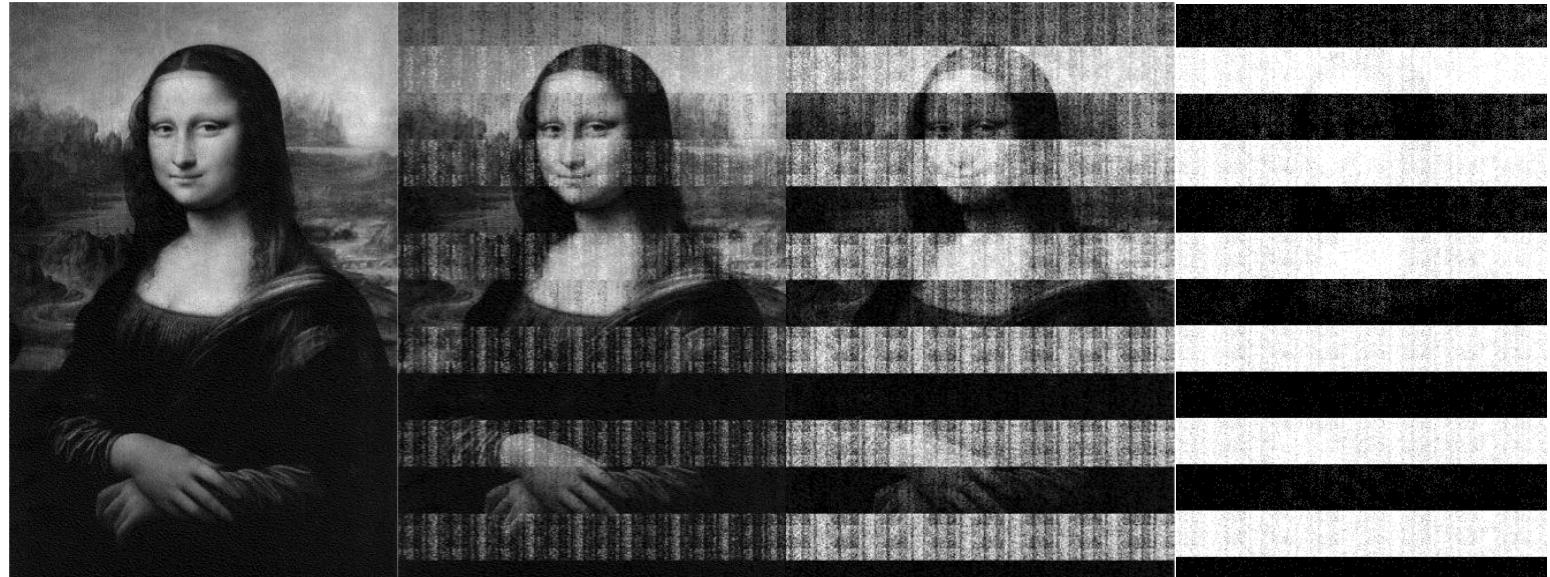
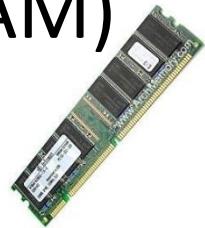


- Hard Disk Encryption available on all major OSs
- Enabled by default on mobile phones
- **Solves Problem:** Good password sufficient for secure storage

# Problem: Physical Attacks

Problem: your key is stored in memory (DRAM)

This happens if you cut power:



5 secs

30 secs

60 secs

300 secs

# Cold Boot Attacks

## Lunchtime Attack:

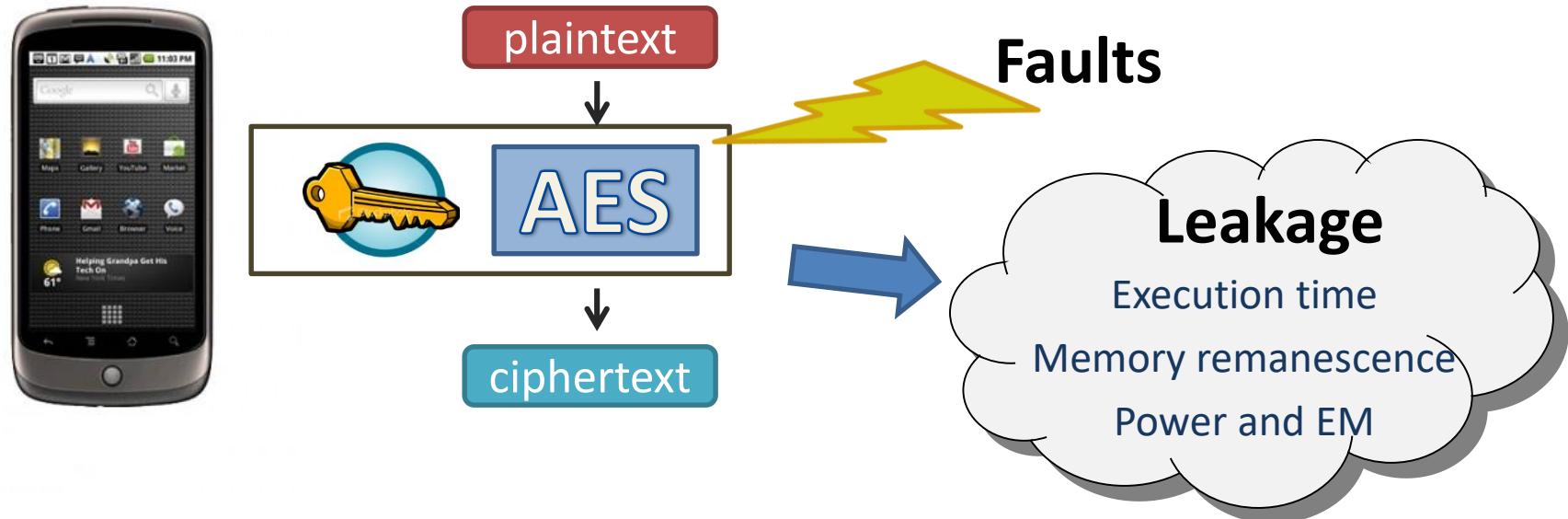
- data will persist for minutes if chips are cooled
- Keys easily recovered from memory content



**Physical Access is needed**

# Implementation Attacks

# Implementation Attacks



- Critical information leaked through side channels
- Adversary can extract critical secrets (keys etc.)
- Usually require physical access (proximity)

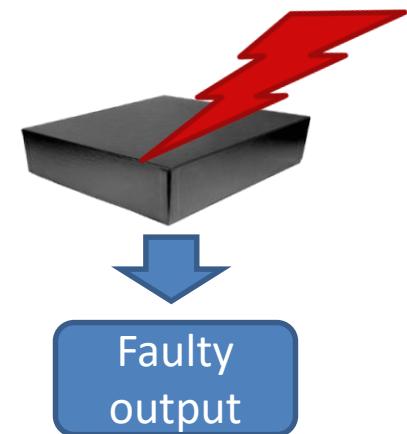
# Physical Attacks

- Invasive Attacks
  - Probing Attacks
- Semi-invasive
  - Fault Injection Attacks
- Non-invasive
  - Timing Attacks (cf. Tuesday talk)
  - Physical side channel attacks:
    - Power, EM, Sound, Light



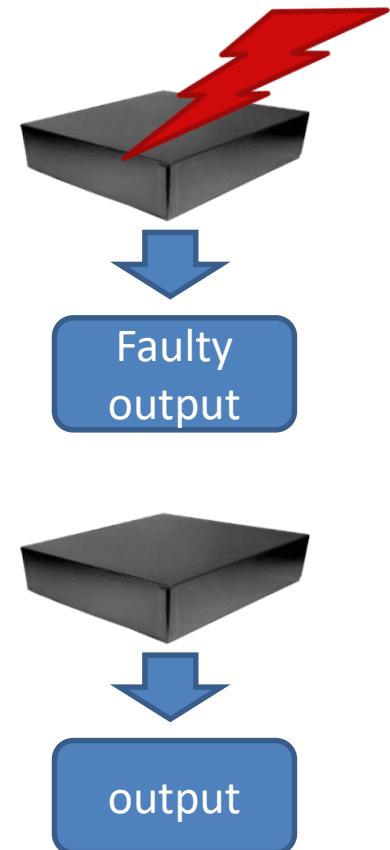
# Fault Attacks

- Very powerful and not that difficult to implement
- **Approach:**
  - Induce faults during crypto computation (e.g. power or clock glitch, shine laser, EM etc.)
  - Use corrupt data output to recover keys
- **Countermeasures:**
  - Strong error detection through coding or repeat computation
  - Tamper resilient hardware
- **Example:** single faulty output of RSA-CRT can reveal entire RSA key [BDL97,Len96]



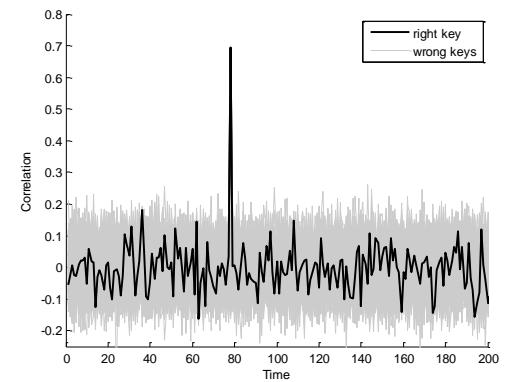
# Types of fault attacks

- Differential Fault Analysis [BS96]:
  - Analyze difference between correct and faulty output: knowledge about fault position and/or value reveals (partial) key
- Simple fault analysis:
  - only faulty output given; additional statistical knowledge about fault behavior needed.
  - Fault sensitivity analysis [LSG10]: only certain internal states can be faulted: faulty behavior → that state occurred



# Information Leakage through Power

- **Key Observation:** Power Consumption of ICs depends on processed data
- First exploited to recover **cryptographic keys** from smart cards in 1999



# Power Consumption of CMOS

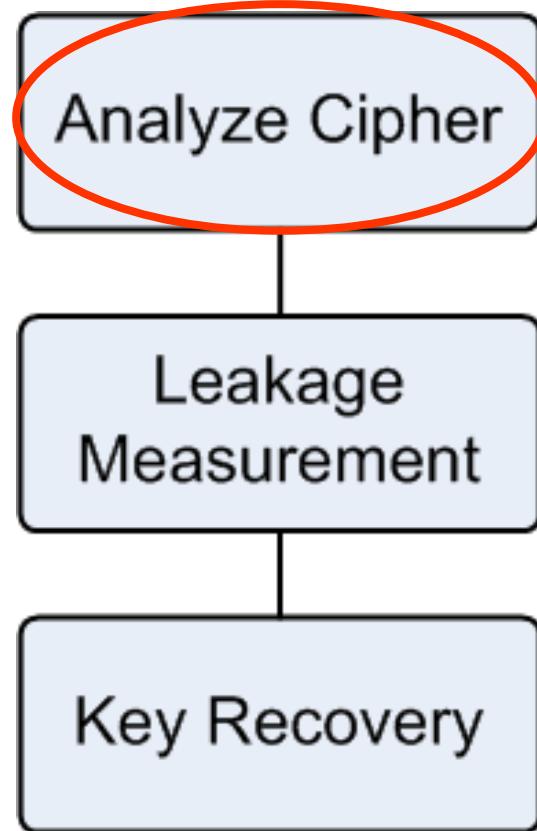
- Information stored as voltage levels – $Hi = 1/Lo = 0$
- Signal transitions dissipate power:

$$P = \underbrace{\alpha \cdot C \cdot V^2 \cdot f}_{dynamic} + \underbrace{V \cdot I_{leak}}_{static}$$

Activity factor  $\alpha$  is determined by data

→ **Power Consumption / EM emanation depends on processed data!**

# A Simple Power Analysis Attack



1. Find a suited predictable intermediate value in the cipher
2. Perform power measurements and post processing
3. Recover Secret Key

# Modular Exponentiation for RSA

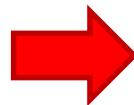
**Basic principle:** Scan exponent bits from left to right and square/multiply operand accordingly → **Exponent is secret key**

## Algorithm: Square-and-Multiply

**Input:** Exponent  $H$ , base element  $x$ , Modulus  $N$

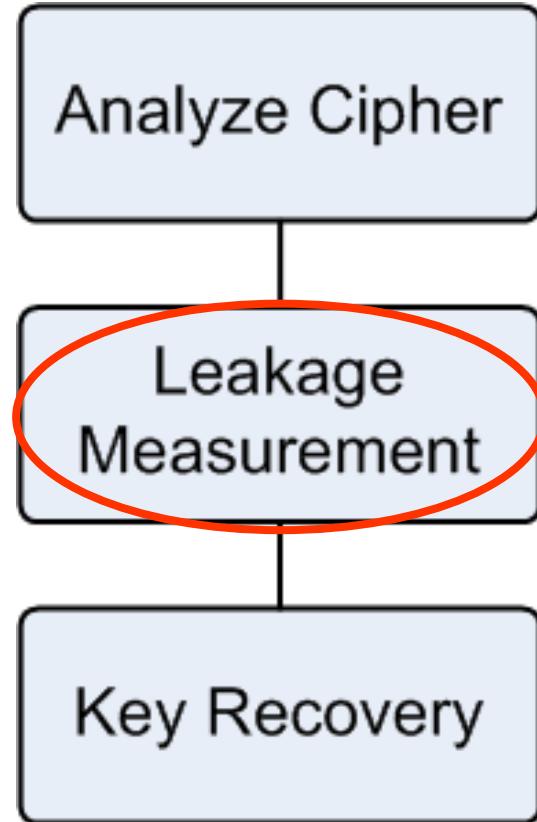
**Output:**  $y = x^H \bmod N$

1. Determine binary representation  $H = (h_t, h_{t-1}, \dots, h_0)_2$
2. **FOR**  $i = t-1$  **TO** 0
3.  $v = v^2 \bmod N$
4. **IF**  $h_i = 1$  **THEN**
5.      $y = y * x \bmod N$
6. **RETURN**  $y$



**Execution of multiply depends on secret**

# A Simple Power Analysis Attack



1. Find a suited predictable intermediate value in the cipher
2. Perform power measurements and post processing
3. Recover Secret Key

# Measurement setup

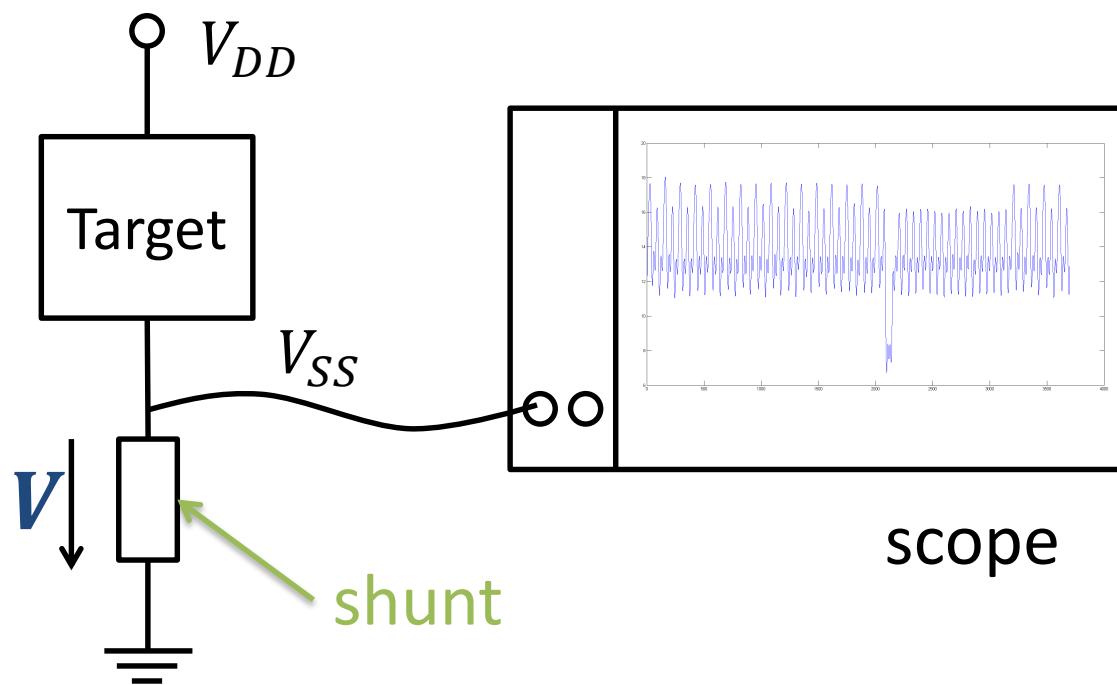


- Oscilloscope measures power or EM from target crypto device
- Usually PC to control setup

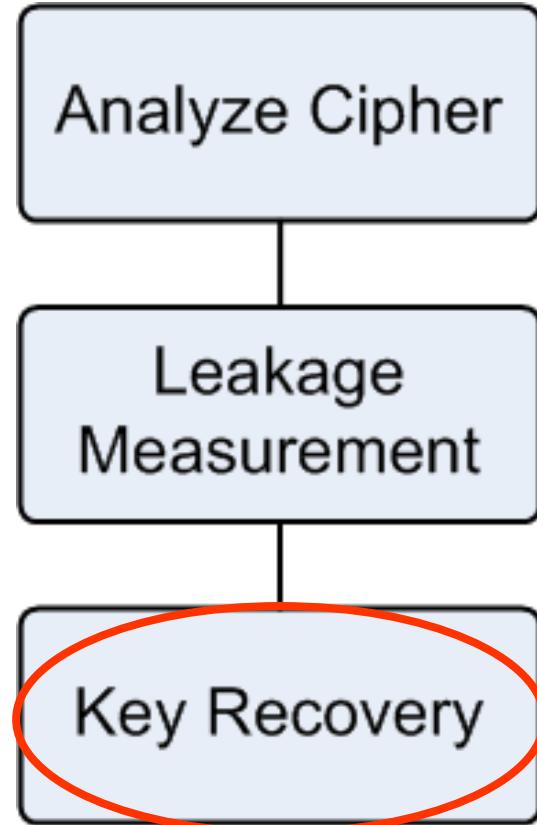


# SPA Measurement Setup

- Voltage drop over shunt resistor  $\sim$  power

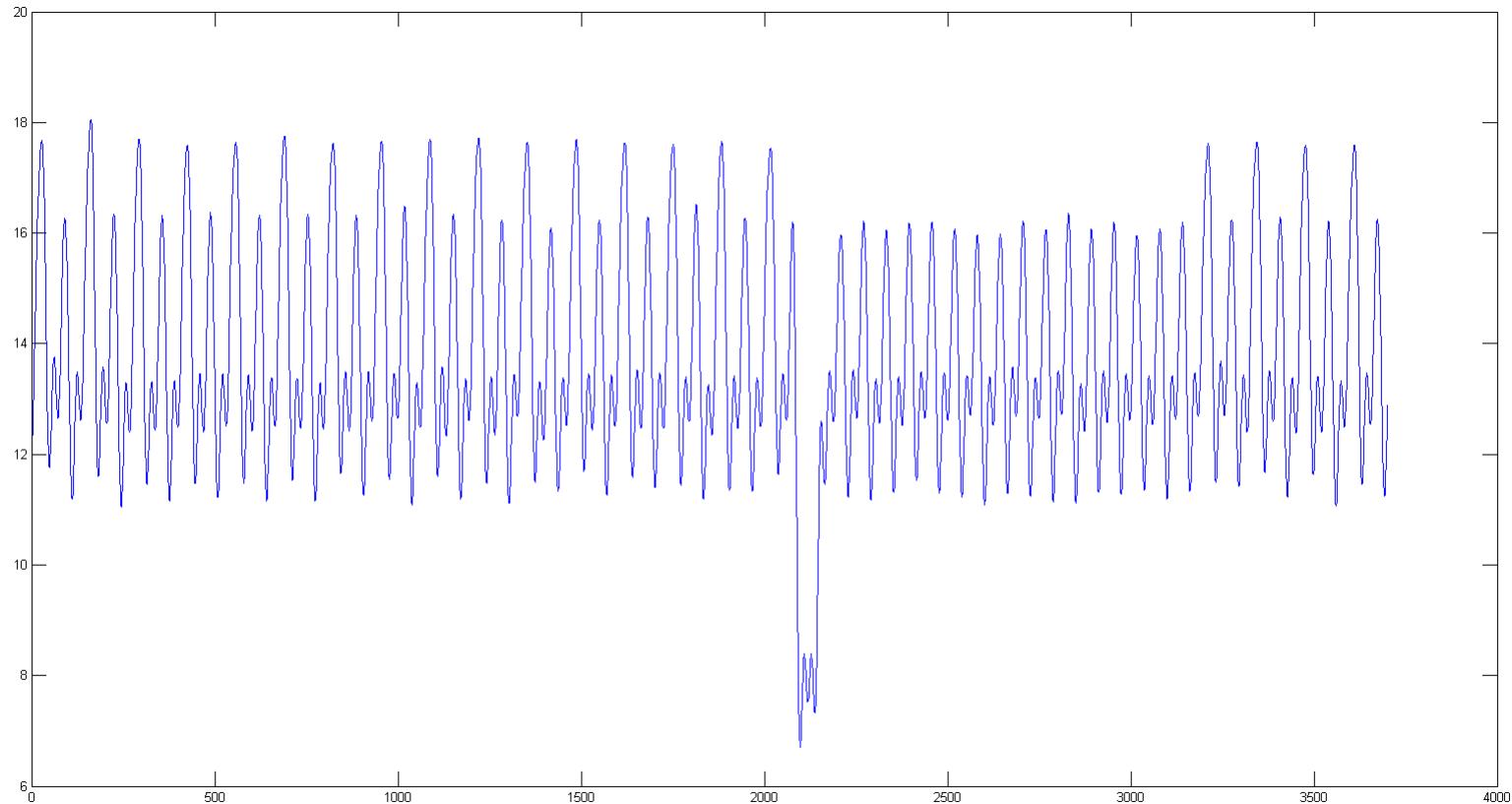


# A Simple Power Analysis Attack



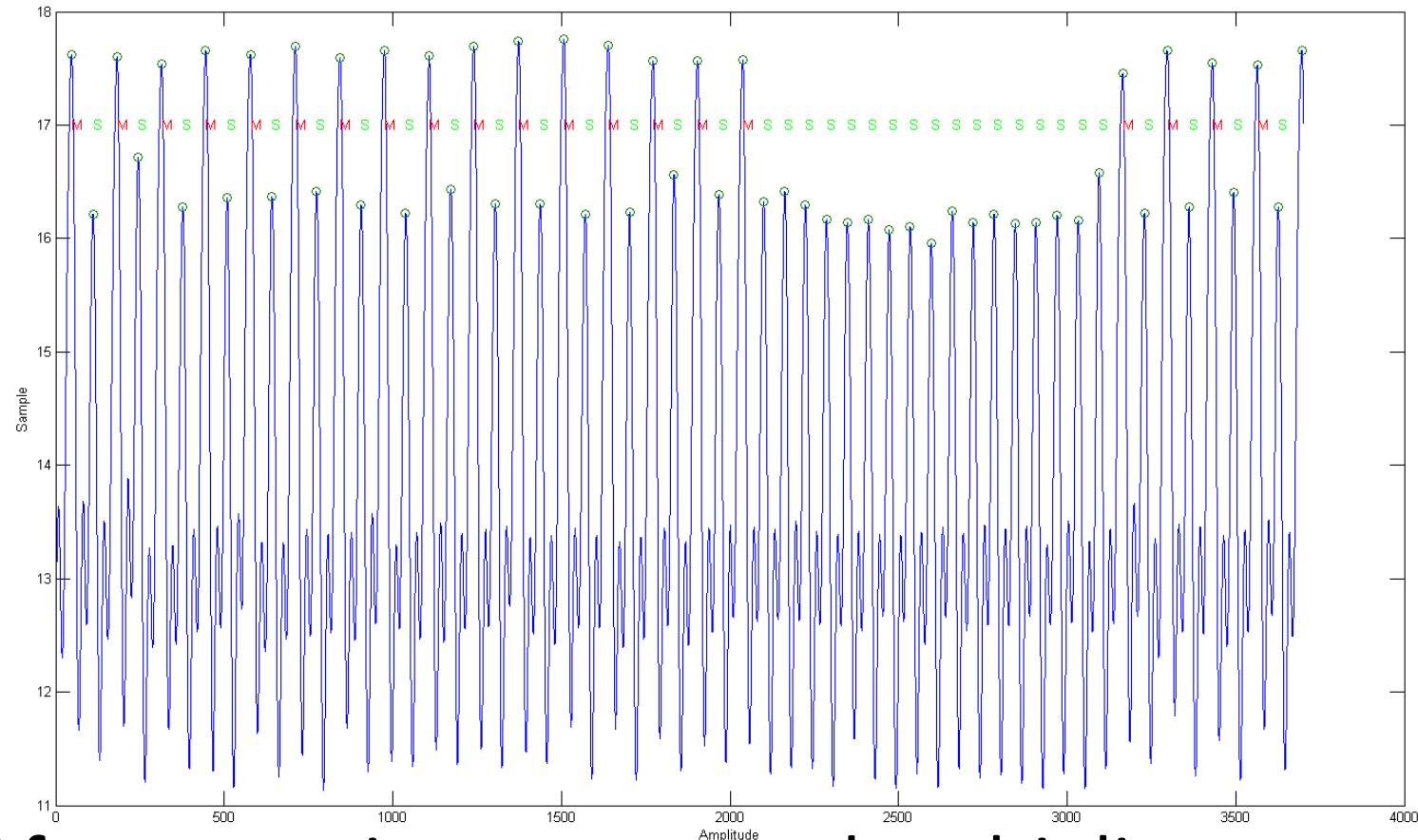
1. Find a suited predictable intermediate value in the cipher
2. Perform power measurements and post processing
3. Recover Secret Key

# RSA Power trace



Where are the squares, where are the multiplies?

# Detecting key bits



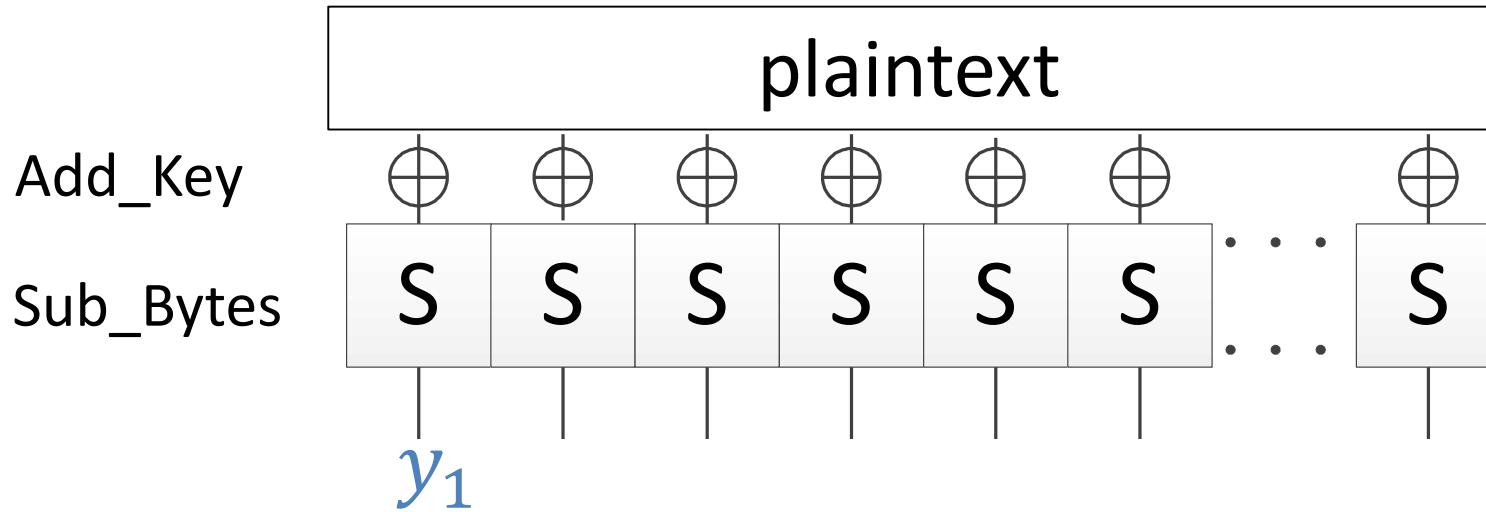
- After zoom-in, squares and multiplies are easily distinguishable

# Differential Power Analysis

- **Key idea:** use statistical information from many observations
- Recall Password Timing Example:  
$$time = f(input, secret)$$
- Leakage exists, how to exploit it?
  - some variations may be predicted
  - variations may be tiny,
  - only small parts of implementation need be predicted



# AES: predicted value



Predicted state:  $y_1 = S(x_1 \oplus key_1)$

Single-bit DPA: Predict only one bit of state:

$$h = \text{LSB}(y_1)$$

# DPA on AES on Controller

Assumption: Controller leaks  $\mathbf{HW}(y_1)$  during S-box lookup

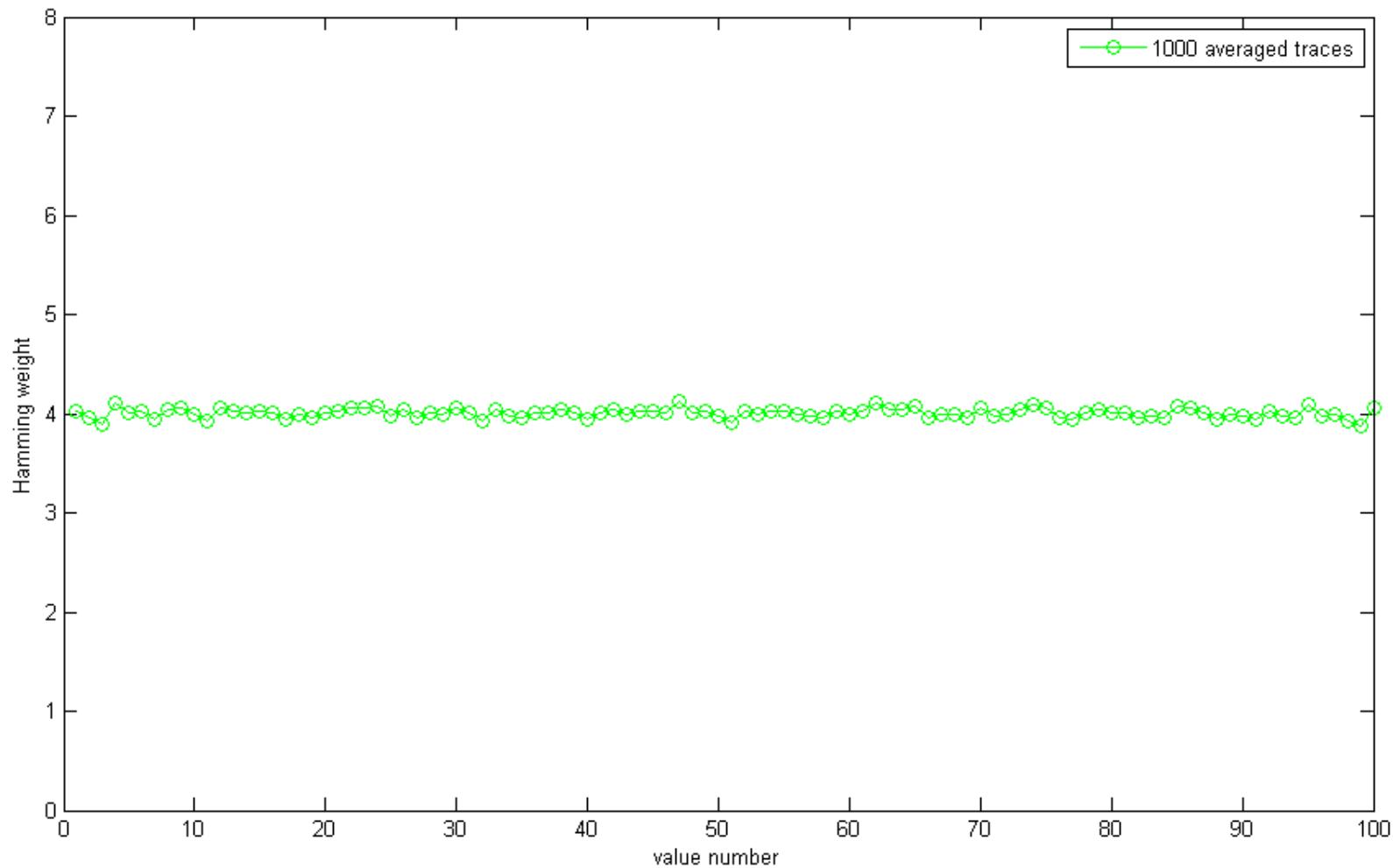
1. Measure  $P_i(t)$  and store all  $\langle P_i(t), in_i \rangle$
2. **Sort** traces based on  $h = \text{LSB}(y_1)$  and average

$$\mu_0 = \overline{P_i(t)} | (h = 0) \quad \mu_1 = \overline{P_i(t)} | (h = 1)$$

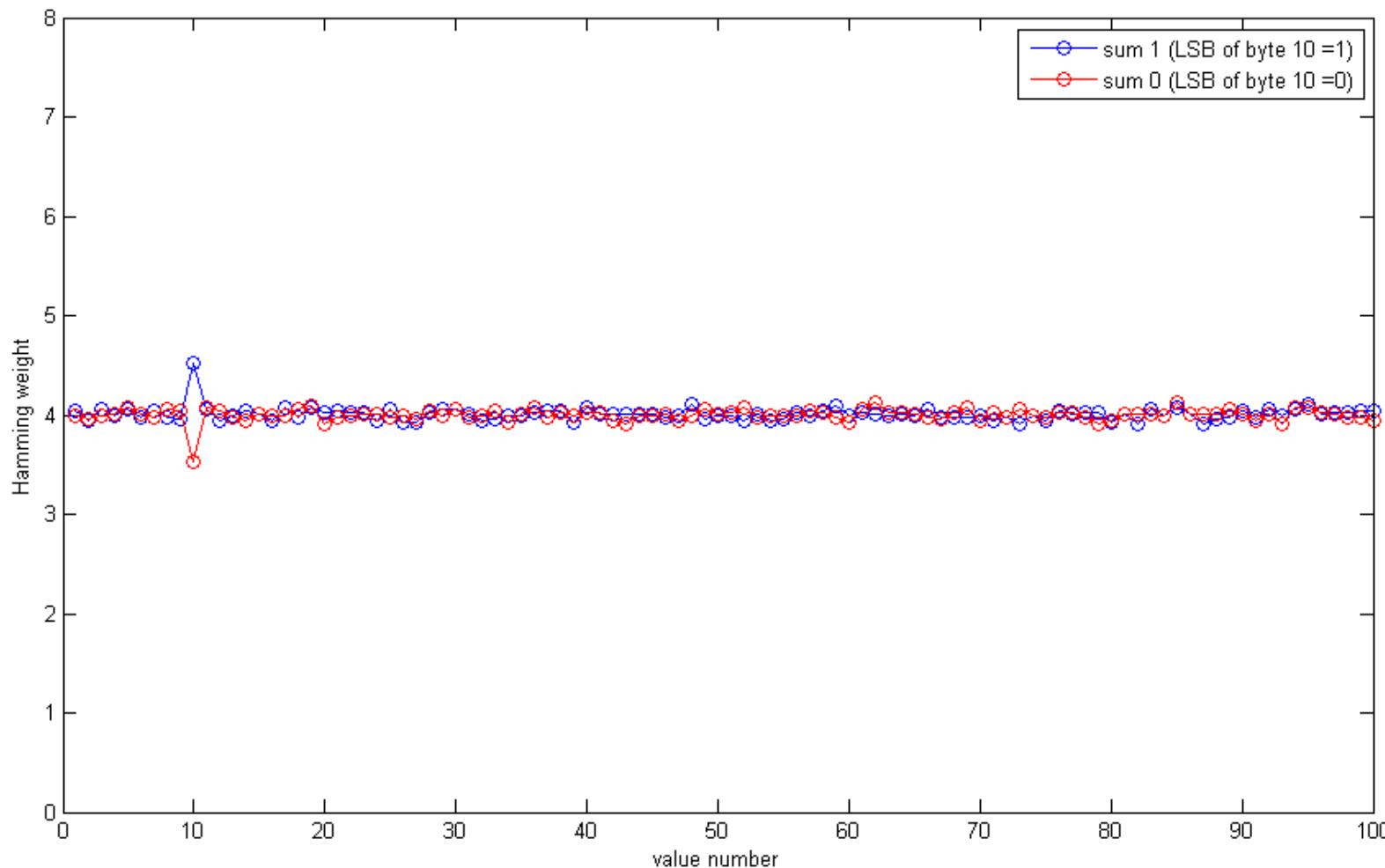
3. Compute **difference of means**:

$$\Delta = \mu_1 - \mu_0$$

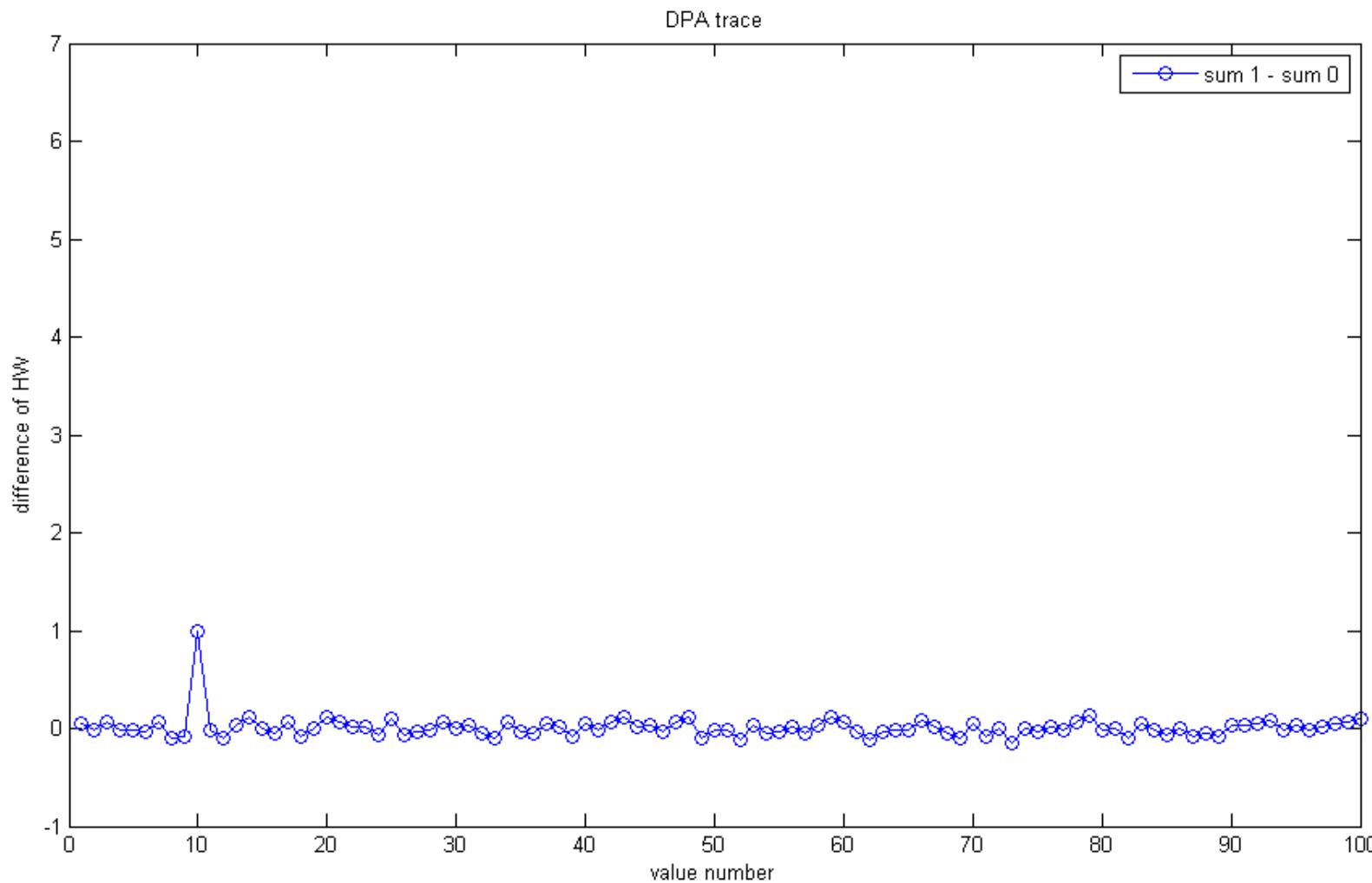
# Average of 1000 HWs



# Sorted Traces (based on $h$ )



# Result of the Distance of Means Attack

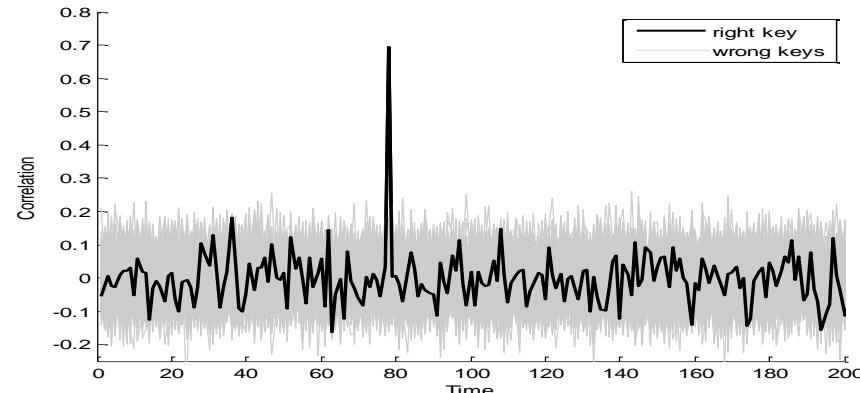


# Side Channel Attacks Classification

- **Non-Profiled Attacks**
  - Need some knowledge of implementation and (approximate) leakage model (or build it on the fly)
    - Difference of Means (Classic DPA)
    - Correlation Power Analysis (CPA)
    - Mutual Information Attack (MIA)
    - Collision Based Attacks
- **Profiled Attacks:**
  - Two-step process: 1) profile leakage, 2) use learned leakage model to extract information
  - Usually more effective in exploitation due to better modeling
    - Template Attack
    - Linear Regression

# Single-bit DPA

- Simple yet effective attack:
  - Very generic leakage model: only needs slight difference for one bit
  - Many more powerful, but less generic attacks exist
- $\Delta \approx 0$  for wrong key and wrong time points
- Reveals both **correct key** AND time point of leakage



# Leakage Detection

# Methods for Leakage Detection?

**Goal:** Simple test to detect any leakage in implementation

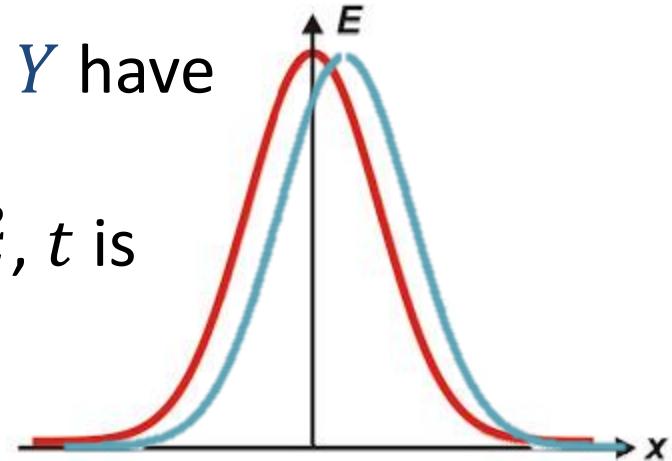
- Profiled vs. Non-profiled?
  - **MIA:** strong but slow convergence; Depends strongly on parameter choices: how to describe and sample pdfs?
  - **Templates:** very powerful, but costly to build and also model-dependent: Which variable to template?
  - Good choices for **leakage quantification**
- **CCA (Correlation Collision Attack)[MME10]:**
  - Basically univariate self-profiling attack
  - Already widely used as leakage detection tool
  - Disadvantage: does not work for single-bit leakages
- Above proposed as attacks. More generic solution?

# Leakage Detection: TVLA Test [GJJR11]

- Builds on **T-Test**: test to check matching means for two distributions
- T-Test returns confidence for non-leakage hypothesis
- Non-profiled, DPA derived
- Originally proposed for automated test suite
  - Given cipher-specific test vectors, check implementation correctness and ensure observed leakage traces do not break test
- Comes in two (three) flavors

# Welch's T-Test

- Checks if two normal distributions  $X, Y$  have the same mean
- With sample mean  $\bar{x}$  and variance  $s_x^2$ ,  $t$  is given as: 
$$t = \frac{\bar{x} - \bar{y}}{\sqrt{\frac{s_x^2}{n_x} + \frac{s_y^2}{n_y}}}$$
- If  $X, Y$  have the same mean, then  $t$  follows a student distribution and thus  $|t|$  is small:  
$$\Pr(|t_{df=v>1000}| > 4.5) < 0.00001$$
- Hence, if no leakage exists, the probability of  $|t| > 4.5$  is sufficiently small



# Fixed vs Random Test

## Non-Specific T-Test

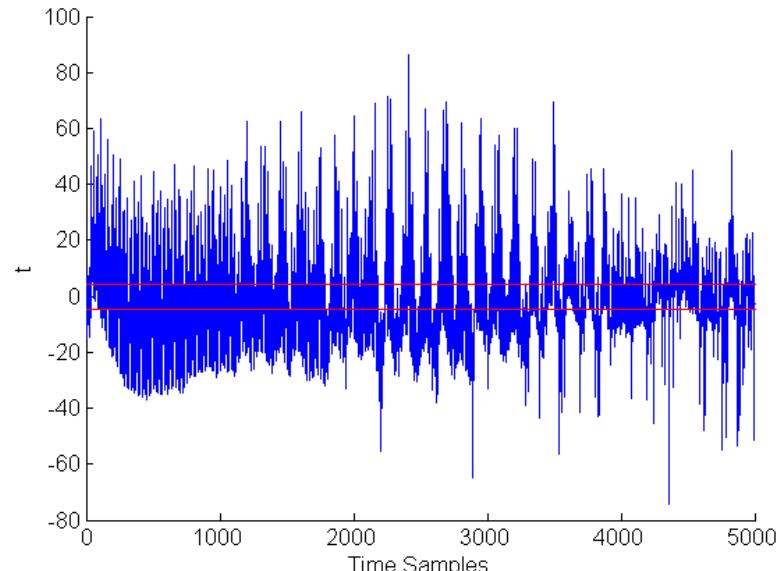
Two sets of measurements:

- **Fixed:** external variables (plaintext, key) are fixed
- **Random:** external variable (e.g. plaintext) is random (others, e.g. key, as before)
- Both sets compared with T-test

→ If (mean of) leakage distributions differ, device leaks

Properties:

- Non-specific: Works on all intermediate states (that differ from mean)
- Not every found leakage might be exploitable



# Random vs. Random Specific T-Test

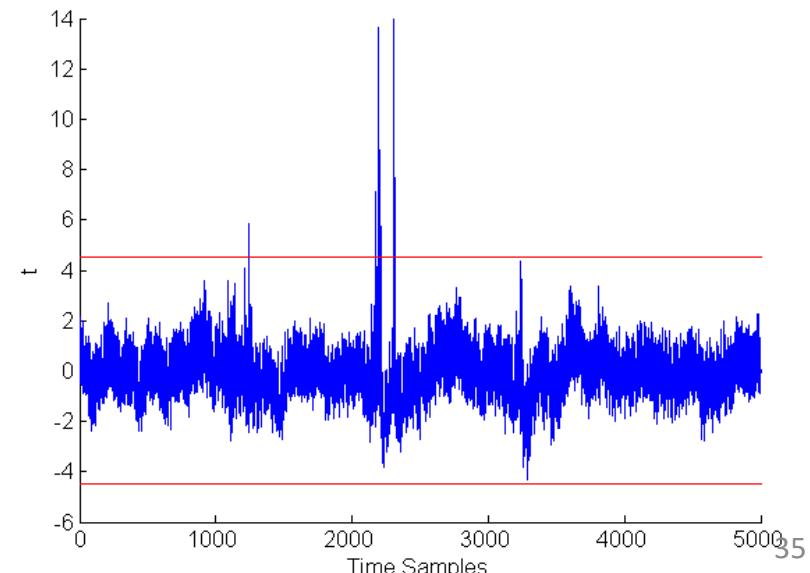
## Kocher's DPA as a Test:

- Key is known and fixed, input is random
- Measurements split in two sets according to known intermediate state
- Both sets compared with T-test

→ If (mean of) leakage distributions differ, **specific intermediate state** leaks

## Properties:

- Specific: Works on predicted intermediate state
- Only finds expected leakages
- Shows an attack



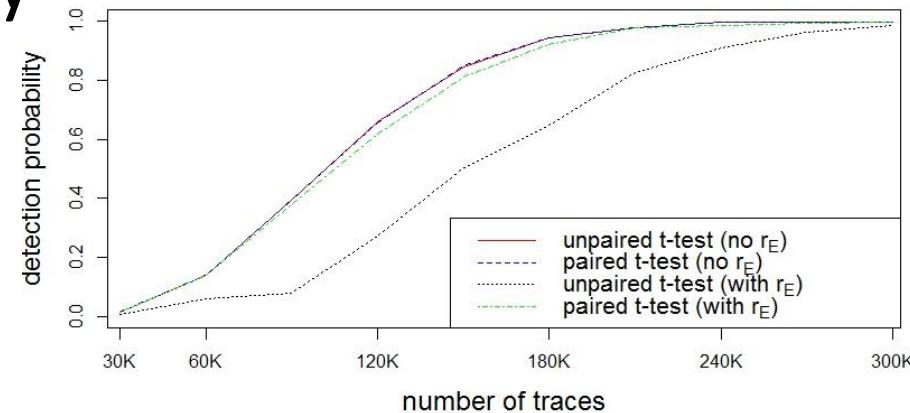
# Practical Considerations

- Test is influenced by measurement setup:
  - Both sets should be **randomly** interleaved, to ensure initial state is not biased
  - FvR: plaintext is fixed in one set, but not other: marks hiding countermeasures as insecure
- Semi-Fixed vs Random Test:
  - Fixes partial intermediate state for semi-fixed case
  - Inputs and outputs still seem random
  - Avoids FvR problem above

# Susceptibility to Common Noise

- Drifts decrease sensitivity
- Remedy: **Paired T-test**

$$t_p = \frac{D}{\sqrt{\frac{s_D^2}{n}}}, \text{ with } D = x_i - y_i$$



- Common noise of paired observations vanishes
- Also works for higher order analysis with *moving averages*
$$x' = (x - \mu_x)^d \rightarrow x' = (x - \mu_{x,local})^d$$
- Less susceptible to noise and easier to compute

# Side Channel Countermeasures

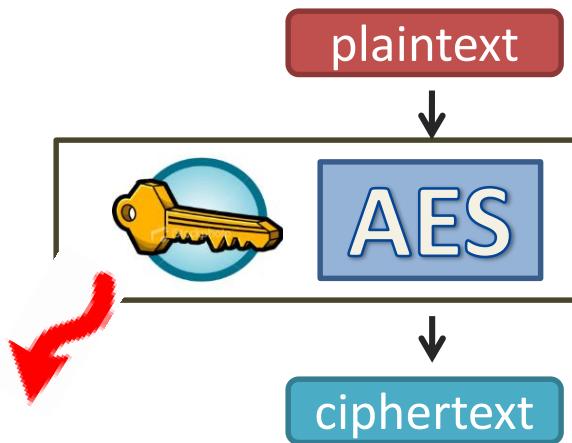
# Preventing Side Channel Attacks

**Goal:** Prevent inference from observable state

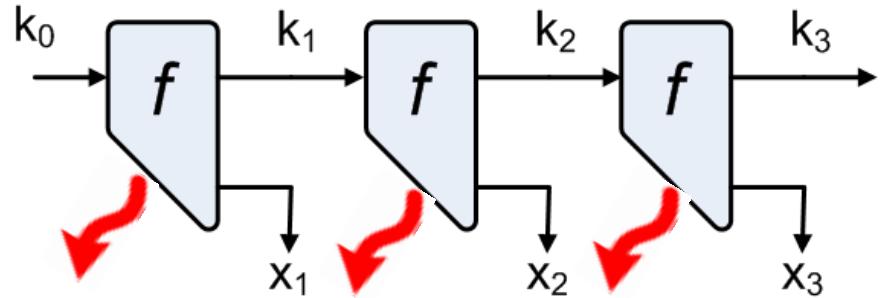
- **Hiding:** lowers signal to noise ratio
  - Noise generator, randomized execution order, dual-rail/asynchronous logic styles...
- **Masking:** (secret sharing) splits state into shares; forces adversary to recombine leakage
  - Boolean or arithmetic masking, Higher-order masking
- **Leakage Resilience:** prevents leakage aggregation by updating secret

# Key usage in Cryptography

## Classic Method:



## Leakage Resilience (Concept):



- Same key leaks for every execution of crypto
- Unlimited observations per key

- Key changes at each iteration
- Only one (few) observation per key

# Leakage Resilience: Key Update

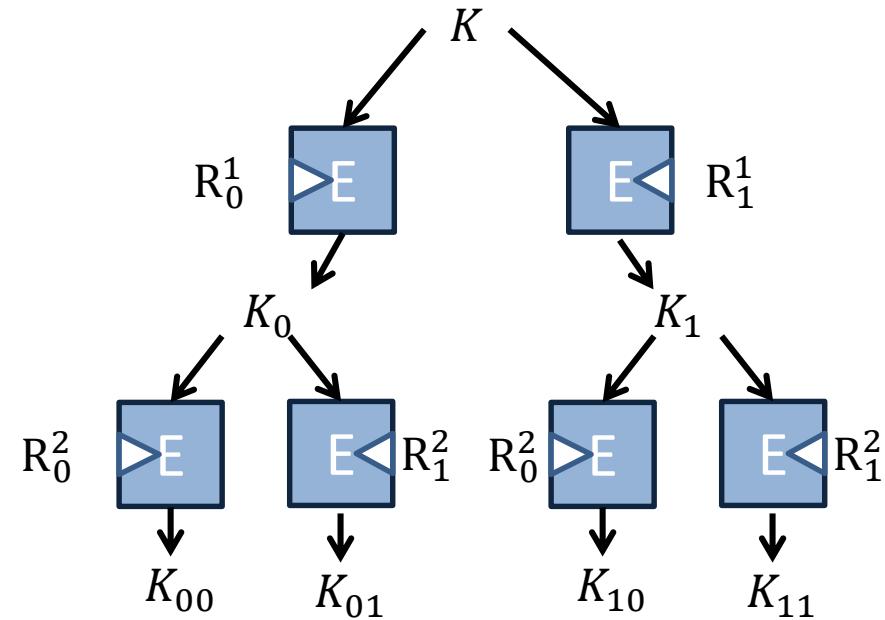
Key needs *update* with every usage:

- **Stateful design**
  - Key owner updates key before each usage
  - **Problem:** Multiple key owners (symmetric crypto) need to stay synchronized
- **Stateless design**
  - Highly desirable for many symmetric applications
  - First practical proposals exist, e.g. [MSJ12] and [TS13]

# Stateless Key Updates

## GGM Construction:

- Nonce bits decide path
- $R_i$ : public randomness
- One encryption per nonce bit (128 Enc)
- Final key  $K_{nonce}$  used!



- Great leakage properties:  
At most two observations per key!
- Big performance overhead: 128 Encryptions to derive key

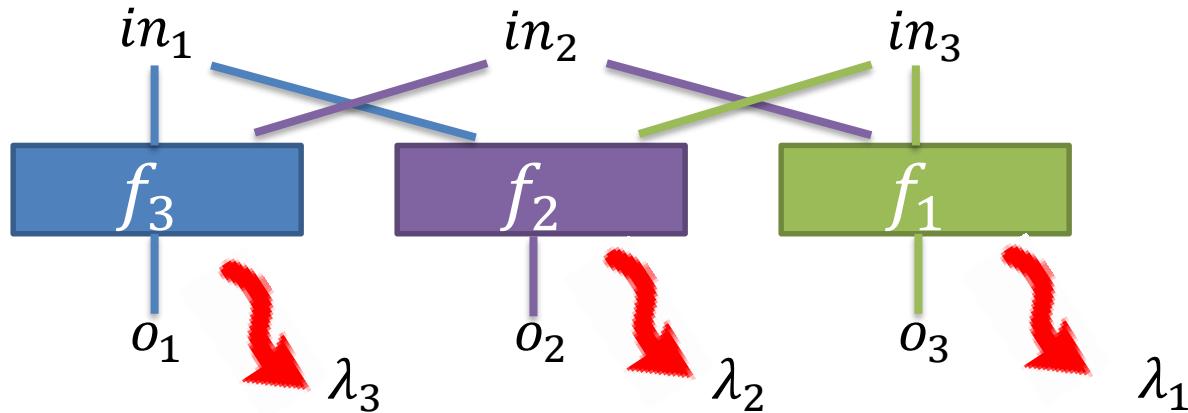
# Masking: Threshold Implementation

# Threshold Implementation [NRR06]

**Applies xor-secret sharing (Boolean masking) to thwart SCA:**

1. Share inputs, states, outputs as  $x = x_1 + x_2 + \dots$ , where  $x_i \in \{0,1\}$  and  $x_i$  must be **uniformly distributed**  
→ **uniformity property**
2. Perform arithmetic on shares without leaking secret;  
Output shares must be independent of at least one input share  
→ **non-completeness property**
3. The correct output is the xor-sum of the shares  
→ **correctness property**
  - Solves the **glitches** issue: any RTL block is independent of at least one share
  - Ensures constant means → prevents 1<sup>st</sup> order DPA leakage

# TI: Parallel vs. Sequential



- Each  $f_i$  lacks one share  $i \rightarrow$  cannot leak about input

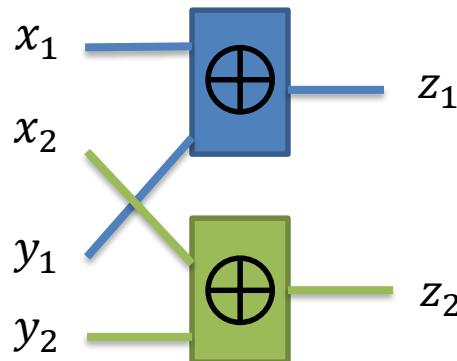
How about parallel leakage?  $\lambda = \sum_i \lambda_i$

- **Uniformity** ensures input-independent mean:
  - First order DPA prevented
  - Aggregate leakage also input-independent mean (as long as  $\lambda_i$  are linearly combined (summed))

# TI: Secure XOR

## Exercise:

- Given  $x = x_1 + x_2$  and  $y = y_1 + y_2$ , compute  $z = z_1 + z_2 = x + y$  without breaking uniformity, non-completeness or correctness?



**Solution:**  $z_1 = x_1 + y_1$

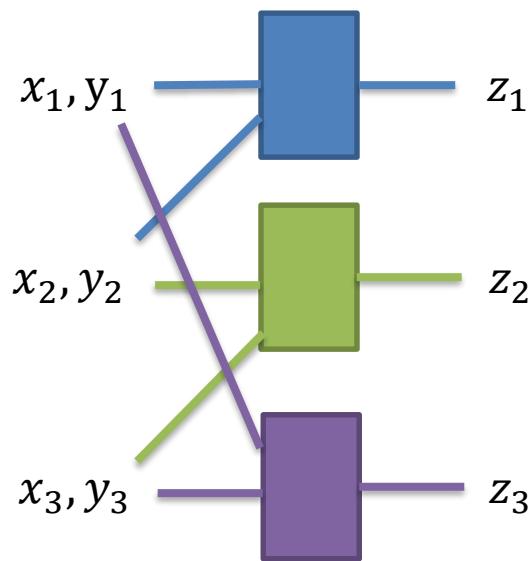
$$z_2 = x_2 + y_2$$

- Correctness:**  $z = z_1 + z_2 = x + y$
- Non-Completeness:**  $i$  share does not depend on non- $i$  shares
- Uniformity:**  $z_i$  is uniform if either  $y_i$  or  $x_i$  is uniform

# TI: Secure AND

## Exercise:

- Given sharing of  $x$  and  $y$ , find minimum number of shares and method to compute  $z = xy$  without breaking uniformity, non-completeness or correctness?



**Solution:**

$$z_1 = x_1y_1 + x_1y_2 + x_2y_1$$
$$z_2 = x_2y_2 + x_3y_2 + x_2y_3$$
$$z_3 = x_3y_3 + x_3y_1 + x_1y_3$$

- Correctness:**  
 $z = z_1 + z_2 + z_3 = xy$
- Completeness:**  
 $i$  share independent of share  $j \neq i$
- Uniformity: not fulfilled!!!**

Uniformity needs more shares or masking variable

# Secure AND: Re-masking

## Restoring uniformity:

- **Add randomness:**

e.g.  $r_1, r_2 \leftarrow \{0,1\}$ ;  $r_3 = r_1 + r_2$

Then:

$$\begin{aligned} z_1 &= x_1y_1 + x_1y_2 + x_2y_1 + \mathbf{r}_1 \\ z_2 &= x_2y_2 + x_3y_2 + x_2y_3 + \mathbf{r}_2 \\ z_3 &= x_3y_3 + x_3y_1 + x_1y_3 + \mathbf{r}_3 \end{aligned}$$

→ Each  $z_i$  is uniformly distributed, non-complete and correct, but additional randomness needed

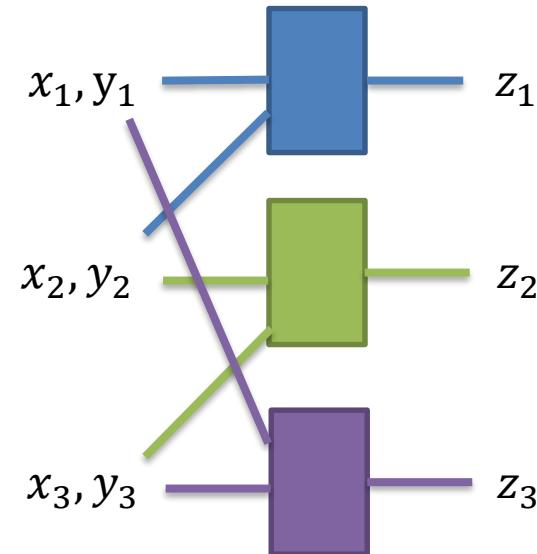
- **Adapt function:**

$z = xy + w$ , (w is properly shared, i.e. uniform):

Then:

$$\begin{aligned} z_1 &= x_1y_1 + x_1y_2 + x_2y_1 + \mathbf{w}_1 \\ z_2 &= x_2y_2 + x_3y_2 + x_2y_3 + \mathbf{w}_2 \\ z_3 &= x_3y_3 + x_3y_1 + x_1y_3 + \mathbf{w}_3 \end{aligned}$$

→ Each  $z_i$  is uniformly distributed, non-complete and correct; randomness of w re-used



# From 3-share to 2-share

Non-linear function:  $z = a \cdot b + c$

$$z_2 = (a_2 \cdot b_2 + c_2) + a_1 \cdot b_2$$

$$z_1 = (a_1 \cdot b_1 + c_1) + a_2 \cdot b_1$$

## Pipelining!

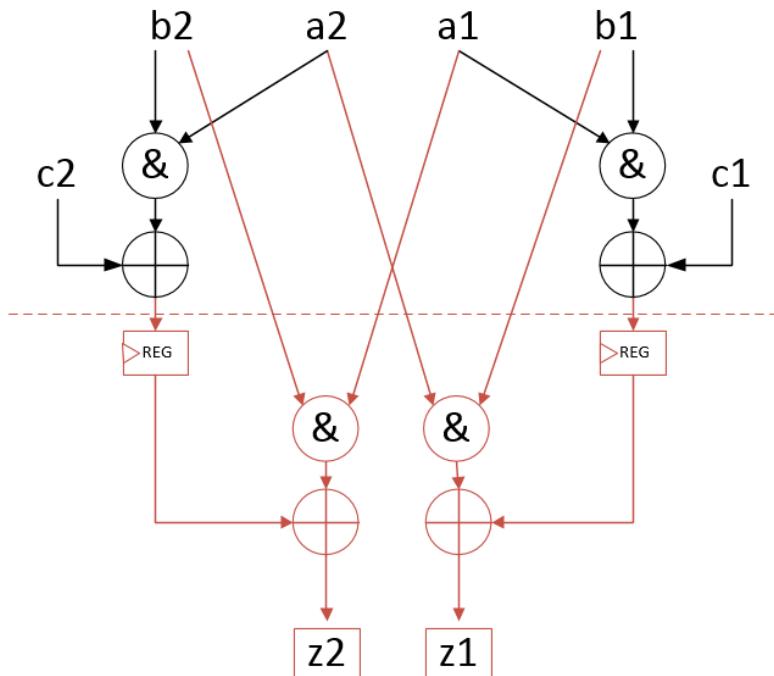
Correct;

Non-Complete;

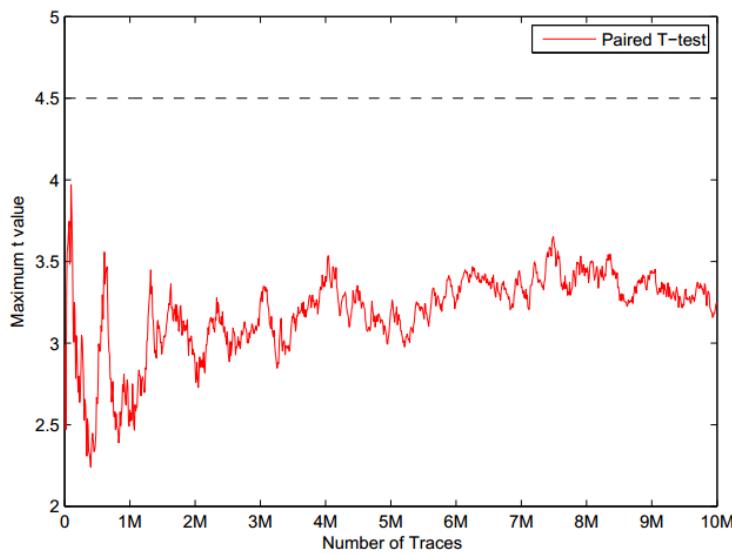
Uniform;

Compared with 3-share:

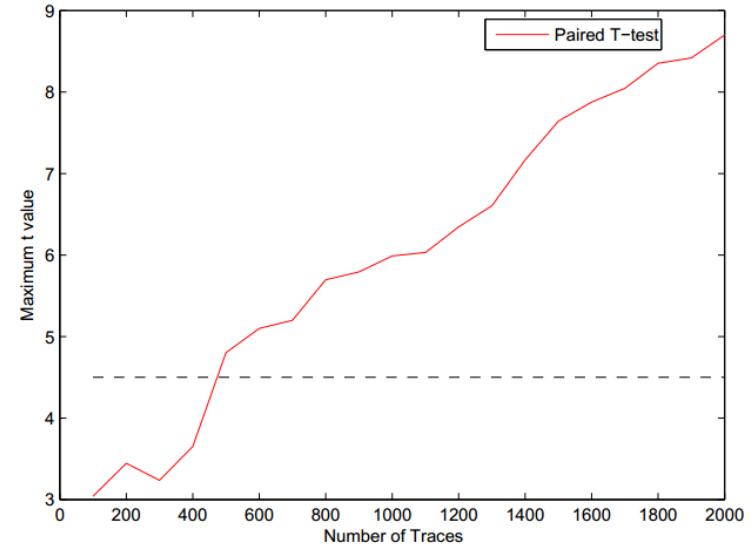
- Less randomness
- Fewer logic operations
- Two extra flip-flops
- Two stages



# Leakage Detection on 2-TI Simon Implementation



(a) 1st order t-test



(b) 2nd order t-test

# Conclusions

- Physical access gives rise to many possible attacks
- Protection against physical attacks is possible, but neither easy nor cheap
  - Perfect protection is not possible
  - device compromise may not result in system compromise
- IoT will ensure interest for years to come

A photograph of the Holstentor, a medieval brick gate in Lübeck, Germany. The gate features two large, round towers with conical roofs. The central section has a balcony with a decorative brick facade. The text "CONCORDIA DOMI FORIS PAX" is visible above the central arch. The sky is clear and blue.

# Thank You!

vernam.wpi.edu

its.uni-luebeck.de

thomas.eisenbarth@uni-luebeck.de